## 3 (Sem-6/CBCS) PHY HE 5

## 2023

## **PHYSICS**

(Honours Elective)

Paper: PHY-HE-6056

(Classical Dynamics)

Full Marks: 80

Time: Three hours

## The figures in the margin indicate full marks for the questions.

Answer the following questions :

 $1 \times 10 = 10$ 

- (a) What is conservative force? Give examples.
- (b) A gas particle is moving inside a sphere, what will be the type of the constraint in it?
- (c) What will be the number of generalized coordinates of a system of N particles having k constraints of motion?

- (d) Calculate the potential energy function associated with the force  $\vec{F} = -yz\hat{i} - zx\hat{j} - xy\hat{k}$ .
- Write down the equation of stable equilibrium of system executing small oscillations.
- Under what condition Galilean transformation reduces to Lorentz transformation?
- Justify that the earth is not an inertial frame.
- State the basic postulates of relativity.
- What is critical velocity of a fluid? Write down its expression in terms of Reynold's number.
- Define terminal velocity of an object falling through a fluid.
- 2. Answer the following questions:

 $2 \times 5 = 10$ 

(a) What are generalized coordinates? If a generalized coordinate has the dimension of momentum, what would be the dimension of generalized velocity?

- (b) Write the Lagrangian of a charged particle in an electromagnetic field, explaining each term.
- (c) Explain: (i) normal modes of vibration; (ii) normal coordinates and (iii) normal frequencies of a system which undergoes small oscillations.
- 1 kg of a substance is fully converted (d) into energy. Calculate the amount of energy produced.
- Show that the velocity of flow is inversely proportional to the area of cross-section of the tube.
- 3. Answer the following: (any four)

 $5 \times 4 = 20$ 

- Show that the path of a charged particle (a) moving perpendicular to an uniform electric field is parabolic in nature.
- (b) Write down the Lorentz transformation equations and obtain Lorentz-Fitzgerald contraction formula.

A massless spring of force constant k has masses  $m_1$  and  $m_2$  attached to its two ends. The system rests on frictionless horizontal plane. Show that the angular frequency of the system is

$$\sqrt{\frac{k}{\mu}}$$
 where  $\mu = \frac{m_1 m_2}{m_1 + m_2}$ .

- What is relativistic energy? Show that the relativistic energy E of a particle is given by is  $E^{2} = p^{2}c^{2} + m^{2}c^{4}$ .
- Explain relativistic time dilation. A certain particle has a life time of 10<sup>-6</sup> sec when measured at rest. How far does it go before decaying if its speed is 0.9c when it is created (c is the velocity of light in free space)?
- Obtain the equation of continuity for an incompressible fluid. An incompressible fluid is flowing through a pipe. If the diameter of the pipe is doubled, what change will occur to the velocity of the fluid?

- 4. Answer the following: (any four) 10×4=40
  - (a) Obtain Lagrange's equation of motion from D'Alembert's principle. Consider a particle of mass m moving in a plane in a central force field. Write its Lagrangian in plane polar co-ordinates. Write the equations of motion and obtain the differential equation of the orbit. 5+5=10
  - Derive Hamilton's canonical equation of motion from Hamilton's principle of least action. A mass m is suspended by a massless spring of spring constant k. The suspension point is pulled upwards with constant acceleration  $a_0$ . Find the Hamiltonian of the system and Hamilton's equations of motion. Also find the equation of motion of the system. 5+5=10
  - Deduce Newton's second law of motion from Hamilton's principle. Masses m and 2m are connected by a light inextensible string which passes over a pulley of radius a. Write the Lagrangian and find the acceleration of the system.

5+5=10

- (d) Derive the velocity addition theorem using four vectors. A particle of rest mass  $1.67 \times 10^{-27} kg$  moves with a velocity  $\sqrt[c]{2}$ . Calculate its relativistic momentum, kinetic energy and total energy. 6+4=10
- (e) Establish Einstein's mass-energy equivalence principle  $E = mc^2$ . A pion decays into a muon and a neutrino. Show that momentum of muon is given

by 
$$p_{\mu} = \frac{c \left(m_{\mu}^2 - m_{\pi}^2\right)}{2m_{\pi}}$$
. 6+4=10

(f) State and explain relativistic transverse Doppler effect. Explain blue shift and red shift in Doppler effect. Calculate the wavelength shift in the relativistic Doppler effect for the frequencies  $H_{\alpha}$  line (6563Å) emitted by a star receding from the earth with a relative velocity 0.1c. Is the classical result (first order) a good approximation? 2+3+5=10

- (g) Derive Poiseuille's equation for the rate of flow of fluid through a capillary tube. A tube of 0.1 cm in diameter and 40 cm long has to deliver 20 kg water in 25 min. Calculate the constant pressure head to be maintained. The coefficient of viscosity for water is 8.9 × 10<sup>-4</sup> N-s-m<sup>-2</sup>.

  6+4=10
- (h) What is Reynold's number? Mention various range of values of Reynold's number for different types of flow of fluid. Derive the Navier-Stokes equation for flow of a viscous fluid.

  1+3+6=10