3 (Sem-5/CBCS) PHY HC 1

momentum 82023 mutum system be

specified similtaneously? Give reason.

Modeline Tegri (Honours Core)

Paper: PHY-HC-5016

(Quantum Mechanics and Applications)

Full Marks: 60

Time: Three hours

The figures in the margin indicate full marks for the questions.

- 1. Answer the following questions: $1 \times 7 = 7$
 - (a) Why eigenvalues and eigenfunctions of Hermite operators are very important for a quantum physicist?
 - (b) Stationary states are those for which the probability density ρ is
 - (i) time-dependent
- 8=4×Q (ii) a time-independent of the toward
 - (iii) space-dependent
 - (iv) space-independent

- (c) Why $\psi = x^n$ is not an acceptable wave function?
 - (d) Can kinetic energy and linear momentum of a quantum system be specified simultaneously? Give reason.
 - (e) Write down the Schrödinger equation for a particle in a square well potential of infinite depth.
 - (f) The z-component of spin angular momentum can take values:
 - Time: Three hough (i)
 - (ii) $\pm \frac{\hbar}{2}$ part for example of $\frac{\hbar}{2}$
 - Answer the following quest # ±18 (iii)
- Why eigenvalues and \$4 \pm (vi) ctions of
 - (g) An atomic state is denoted by $^4D_{5/2}$. What should be the minimum number of electrons involved for this state?
- 2. Answer the following questions: 2×4=8
 - (a) Show that $[\hat{L}_x, \hat{L}_y] = i\hbar \hat{L}_z$.

- (b) How much energy is released, when a 3d electron in the hydrogen atom makes a transition to a 2p state?
- (c) Calculate Lande's g factor for a p-electron.
- (d) Show that in a non-dispersive medium, the group velocity is equal to the phase velocity.
- 3. Answer any three of the following questions: 5×3=15
 - (a) What do you mean by dynamical variables and expectation value of a dynamical variable? Obtain quantum mechanical operators corresponding to linear momentum, kinetic energy and Hamiltonian of a system. 1+1+3=5
 - (b) A free particle is initially localized in the range -a < x < a as:

$$\psi(x, 0) = u(x) = A$$
, $-a < x < 0$
 $u(x) = 0$, otherwise

where A, a are real and positive. Find $\psi(x,t)$.

- (c) Starting from time independent Schrödinger equation in polar coordinate for hydrogen atom, show that for azimuthal angle, the probability density of electron is constant. What is its significance?
 - (d) A particle in the ground state is located in one dimensional potential well of width L with absolutely impenetrable walls 0 < x < L. Find probability of finding the particle in the region wol $\frac{L}{3} < x < \frac{2L}{3}$. So the contraction of the second se
- (e) What are identical particles? Show that when two identical particles try to occupy same quantum state, then antisymmetric wave function becomes zero. Why Pauli's exclusion principle is not valid for Bosons? 1+3+1=5 Hamiltonian of a system. 1+1+3=5
- Answer any three of the following 10×3=30 questions:
 - (i) Explain the meaning of probability (a) current density for a quantum system. Deduce an expression for the probability current density for three dimensional motion and the law of conservation of probability 1+3+1=5density.

(ii) The wave function of a particle moving in one dimension is given to be to classical

$$\psi(x) = \begin{cases} \sqrt{\frac{15}{a}} A(a^2 - x^2) & \text{for } -a \le x \le 0\\ 0 & \text{for } |x| > a \end{cases}$$

Find the value of A that will normalise $\psi(x)$ and calculate the expectation values of x and p.

5=2+2+1 An spectrometer can resolve

[where the notations have their eved IIIw bi usual meaning.

- (b) (i) For a linear harmonic oscillator, obtain the ground state wave function. Make a plot of the first and second energy eigenfunctions. 7+1=8
- (ii) Compare the ground state classical and quantum mechanical probability of the oscillator. What and appens when the quantum pand doing numbers become very large?

(c) From the polar equation of hydrogen atom separate the radial part and using Frobenius method find the energy 3+7=10states.

- (d) (i) What is Zeeman effect? Give the explanation of normal Zeeman effect on the basis of classical theory and obtain an expression for Zeeman shift.

 1+5=6
- (ii) Explain why normal Zeeman effect occurs only in atoms with even number of electrons.
- spectral lines separated by 0.03nm.

 How much magnetic field will have to be applied to a source of 422.7nm line, so that the triplet is just resolved in normal Zeeman effect?

(e) Differentiate between L-S and J-J coupling schemes.

The wavelengths of *D* lines of sodium are 5896Å and 5890Å. Calculate the (a) energy of the levels from which these spectral lines originate (b) separation in *eV* between the two *p*-levels in sodium atom. Given that the ionisation energy of sodium is equal to 5·13*eV*.

5+5=10

(f) Describe Stern-Gerlach experiment with a suitable diagram and explain on the basis of quantum theory.

In a Stern-Gerlach experiment silver atoms traverse a distance 0.1m in a non-homogeneous field of gradient 55 Tesla m^{-1} . If the velocity of silver atom is $450ms^{-1}$, calculate the separation between the two traces on the collector plate.

[Bohr magneton = $9.27 \times 10^{-24}JT^{-1}$, Mass of silver atom = $1.79 \times 10^{-25}kg$] 3+5+2=10