1 (Sem-2) STA

2024

STATISTICS

Paper: STA0200104

(Correlation & Regression, Probability Distributions, Statistical Inference-I and Finite Difference)

Full Marks: 45

Time: Two hours

The figures in the margin indicate full marks for the questions.

1.	Answer the following questions: 1×5=5	
	(a)	Karl Pearson's correlation coefficient lies between and
		(Fill in the blanks)
	(b)	For binomial distribution, mean > variance. (true or false)
	(c)	Define level of significance.
	(d)	What is categorical data?
	(e)	What is the relation between Δ and E ?

- 2. Answer any five from the following questions: 2×5=10
 - (a) Write two properties of Karl Pearson's correlation coefficient:
 - (b) Write Simpson's $\frac{1}{3}$ rd rule of numerical integration.
 - (c) Find the mean of binomial distribution.
 - (d) Define type I and type II errors.
 - (e) Why there are two regression lines?
 - (f) Prove that $(1 + \Delta)(1) = 1$
 - (g) Write two properties of Δ and E.
 - (h) Write two instances where Poisson distribution may be employed.
 - (i) For a binomial distribution n = 10 $p = \frac{1}{2}$. Find p(x = 2).
 - (j) If X follows Poisson distribution with $E(X^2) = 6$, find E(X).
- 3. Answer any four questions :

5×4=20

(a) Write a short note on principle of least square.

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- (b) Describe the properties of normal distribution.
- (c) Describe the test of goodness of fit using chi-square test.
- (d) Derive Newton's forward interpolation formula.
- (e) Define divided differences. Prove that the third, divided differences with the arguments a, b, c and d of the function $\frac{1}{x^2}$ is equal to

$$\frac{abc+bcd+dca+abd}{a^2b^2c^2d^2}$$

- (f) Write a short note on 'general quadrature formula' in the case of numerical integration.
- (g) Describe t-test for testing single mean.
- (h) Prove that correlation co-efficient is independent of change of origin and scale.
- 4. Answer any one question from the following:
 - (a) Write a note on scatter diagram.

 Describe how we can study the correlation between two variables with the help of scatter diagram.

- (b) Define Poisson distribution. Derive the distribution as a limiting case of binomial distribution.
- (c) Describe the properties of divided differences and prove any one of them.
- (d) Explain the test of significance for an observed proportion in case of large sample. A coin was tossed 100 times and 75 heads were observed. Test whether the coin is unbiased.